

**SECTION 1A: INTEGER ADDITIONS**

All answers are required to their full accuracy

- |      |             |             |             |             |             |           |       |       |              |    |
|------|-------------|-------------|-------------|-------------|-------------|-----------|-------|-------|--------------|----|
| 1 )  | 28 +        | 73          | =           | _____       | 1           |           |       |       |              |    |
| 2 )  | 88 +        | 79          | =           | _____       | 1           |           |       |       |              |    |
| 3 )  | 211 +       | 774         | =           | _____       | 1           |           |       |       |              |    |
| 4 )  | 197 +       | 765 +       | 456         | =           | _____       | 2         |       |       |              |    |
| 5 )  | 71159 +     | 44872       | =           | _____       | 2           |           |       |       |              |    |
| 6 )  | 3613 +      | 7780 +      | 7666 +      | 3805        | =           | _____     | 3     |       |              |    |
| 7 )  | 1409556 +   | 5708110     | =           | _____       | 3           |           |       |       |              |    |
| 8 )  | 312696 +    | 157988 +    | 39406       | =           | _____       | 3         |       |       |              |    |
| 9 )  | 5677472 +   | 6061440 +   | 4261931     | =           | _____       | 4         |       |       |              |    |
| 10 ) | 1393541 +   | 7949113 +   | 2929768 +   | 9588175     | =           | _____     | 5     |       |              |    |
| 11 ) | 3586660 +   | 3118984 +   | 8708382 +   | 6487108 +   | 8139930     | =         | _____ | 6     |              |    |
| 12 ) | 15448525 +  | 10079131 +  | 8841416 +   | 23723332 +  | 12390451    | =         | _____ | 7     |              |    |
| 13 ) | 993989099 + | 535271927 + | 496688279 + | 869260289 + | 249755313 + | 163453114 | =     | _____ | 9            |    |
|      |             |             |             |             |             |           |       |       | Total value: | 47 |

## **SECTION 1B: INTEGER SUBTRACTIONS**

All answers are required to their full accuracy

- |      |                 |   |                 |   |       |   |
|------|-----------------|---|-----------------|---|-------|---|
| 1 )  | 71              | - | 10              | = | _____ | 1 |
| 2 )  | 97              | - | 6               | = | _____ | 1 |
| 3 )  | 109             | - | 22              | = | _____ | 1 |
| 4 )  | 2658            | - | 1289            | = | _____ | 1 |
| 5 )  | 66500           | - | 22761           | = | _____ | 1 |
| 6 )  | 29073           | - | 1736            | = | _____ | 1 |
| 7 )  | 787689          | - | 426548          | = | _____ | 2 |
| 8 )  | 509760          | - | 256320          | = | _____ | 2 |
| 9 )  | 5329312         | - | 811245          | = | _____ | 2 |
| 10 ) | 6509742         | - | 501794          | = | _____ | 2 |
| 11 ) | 22654155        | - | 4974887         | = | _____ | 2 |
| 12 ) | 993159751       | - | 243620191       | = | _____ | 3 |
| 13 ) | 3383770412      | - | 1424443684      | = | _____ | 3 |
| 14 ) | 41175187976     | - | 1923462994      | = | _____ | 4 |
| 15 ) | 418385157201    | - | 212318554321    | = | _____ | 4 |
| 16 ) | 1986212852925   | - | 1059543012670   | = | _____ | 5 |
| 17 ) | 568638515612928 | - | 406919243254703 | = | _____ | 6 |
| 18 ) | 456648535251072 | - | 316438679442454 | = | _____ | 6 |

Total value: 47

**SECTION 1C: DECIMAL ADDITIONS & SUBTRACTIONS**

All answers are required to their full accuracy

|      |               |               |              |             |           |         |       |       |   |
|------|---------------|---------------|--------------|-------------|-----------|---------|-------|-------|---|
| 1 )  | 3.7 +         | 6.1           | =            | _____       | 1         |         |       |       |   |
| 2 )  | 3.6 +         | 1.1 +         | 8.5          | =           | _____     | 1       |       |       |   |
| 3 )  | 1.2 +         | 6.2 +         | 4.4 +        | 9.4         | =         | _____   | 2     |       |   |
| 4 )  | 9362.5 +      | 602.62        | =            | _____       | 2         |         |       |       |   |
| 5 )  | 339.3 +       | 536.8 +       | 913.4 +      | 968.2 +     | 886.3     | =       | _____ | 3     |   |
| 6 )  | 831347.12 +   | 56891.403     | =            | _____       | 4         |         |       |       |   |
| 7 )  | 801.68 +      | 8575.5 +      | 851.61 +     | 555.82 +    | 1971.4 +  | 276.61  | =     | _____ | 5 |
| 8 )  | 106.547 +     | 765.866 +     | 96017.2 +    | 7914.64 +   | 21874.9 + | 810.863 | =     | _____ | 5 |
| 9 )  | 39477.5633 +  | 41924.42249 + | 76910.9055 + | 60708.73717 | =         | _____   | 6     |       |   |
| 10 ) | 6.6 -         | 5.1           | =            | _____       | 1         |         |       |       |   |
| 11 ) | 69.4 -        | 50.3          | =            | _____       | 1         |         |       |       |   |
| 12 ) | 738.7 -       | 265           | =            | _____       | 1         |         |       |       |   |
| 13 ) | 1609.6 -      | 942           | =            | _____       | 1         |         |       |       |   |
| 14 ) | 4399.01 -     | 2490.79       | =            | _____       | 2         |         |       |       |   |
| 15 ) | 51056.23 -    | 14761.28      | =            | _____       | 2         |         |       |       |   |
| 16 ) | 62828.691 -   | 23606.474     | =            | _____       | 3         |         |       |       |   |
| 17 ) | 622417.157 -  | 131581.347    | =            | _____       | 3         |         |       |       |   |
| 18 ) | 3461280.096 - | 2672905.104   | =            | _____       | 4         |         |       |       |   |

Total value: 47

**SECTION 1D: MIXED ADDITIONS & SUBTRACTIONS**

All answers are required to their full accuracy

- |      |           |           |           |           |         |       |              |    |
|------|-----------|-----------|-----------|-----------|---------|-------|--------------|----|
| 1 )  | 514 -     | 343 +     | 261       | =         | _____   | 2     |              |    |
| 2 )  | 8310 -    | 5032 +    | 7224      | =         | _____   | 2     |              |    |
| 3 )  | 7814 -    | 4560 +    | 5431 -    | 5257      | =       | _____ | 3            |    |
| 4 )  | 6100 -    | 2120 +    | 5166 -    | 3987      | =       | _____ | 3            |    |
| 5 )  | 6233 -    | 2041 +    | 3224 -    | 2787      | =       | _____ | 3            |    |
| 6 )  | 5323 -    | 3130 +    | 4394 -    | 2133      | =       | _____ | 3            |    |
| 7 )  | 9798 -    | 5824 +    | 6195 -    | 5414      | =       | _____ | 3            |    |
| 8 )  | 5729 -    | 3770 +    | 3820 -    | 3195      | =       | _____ | 3            |    |
| 9 )  | 96023 -   | 56408 +   | 58507 -   | 40460     | =       | _____ | 3            |    |
| 10 ) | 33437 -   | 13940 +   | 29595 -   | 15104     | =       | _____ | 4            |    |
| 11 ) | 345787 -  | 223794 +  | 227178 -  | 196624    | =       | _____ | 5            |    |
| 12 ) | 313194 -  | 185078 +  | 256738 -  | 205827 +  | 582372  | =     | _____        | 6  |
| 13 ) | 546368 -  | 308358 +  | 273905 -  | 185713 +  | 599207  | =     | _____        | 6  |
| 14 ) | 437685 -  | 184177 +  | 319420 -  | 291980 +  | 960595  | =     | _____        | 6  |
| 15 ) | 4030063 - | 2414333 + | 3704656 - | 1264988 + | 1667428 | =     | _____        | 7  |
|      |           |           |           |           |         |       | Total value: | 59 |

## **SECTION 2: INTEGER MULTIPLICATIONS**

All answers are required to their full accuracy

- |      |         |   |          |   |       |    |       |    |
|------|---------|---|----------|---|-------|----|-------|----|
| 1 )  | 7       | x | 28       | = | _____ | 1  |       |    |
| 2 )  | 4       | x | 79       | = | _____ | 1  |       |    |
| 3 )  | 70      | x | 51       | = | _____ | 2  |       |    |
| 4 )  | 29      | x | 716      | = | _____ | 4  |       |    |
| 5 )  | 44      | x | 3939     | = | _____ | 5  |       |    |
| 6 )  | 943     | x | 7941     | = | _____ | 6  |       |    |
| 7 )  | 44      | x | 71641    | = | _____ | 6  |       |    |
| 8 )  | 3937    | x | 7799     | = | _____ | 8  |       |    |
| 9 )  | 409     | x | 880105   | = | _____ | 10 |       |    |
| 10 ) | 20119   | x | 95759    | = | _____ | 13 |       |    |
| 11 ) | 3074    | x | 4834133  | = | _____ | 16 |       |    |
| 12 ) | 197821  | x | 6729744  | = | _____ | 20 |       |    |
| 13 ) | 8444448 | x | 75406747 | = | _____ | 25 |       |    |
| 14 ) | 9       | x | 6        | x | 7     | =  | _____ | 1  |
| 15 ) | 8       | x | 28       | x | 16    | =  | _____ | 3  |
| 16 ) | 98      | x | 67       | x | 28    | =  | _____ | 6  |
| 17 ) | 71      | x | 128      | x | 286   | =  | _____ | 12 |
| 18 ) | 327     | x | 376      | x | 9919  | =  | _____ | 18 |
| 19 ) | 575     | x | 233      | x | 3670  | =  | _____ | 18 |
| 20 ) | 535     | x | 7536     | x | 5765  | =  | _____ | 25 |

Total value: 200

**SECTION 3: INTEGER DIVISIONS (EXACT)**

All answers in this section are required to their full accuracy.

- |      |             |   |           |   |       |    |
|------|-------------|---|-----------|---|-------|----|
| 1 )  | 70          | / | 5         | = | _____ | 1  |
| 2 )  | 600         | / | 30        | = | _____ | 1  |
| 3 )  | 8500        | / | 85        | = | _____ | 2  |
| 4 )  | 91020       | / | 6068      | = | _____ | 3  |
| 5 )  | 795984      | / | 7107      | = | _____ | 4  |
| 6 )  | 5180598     | / | 81        | = | _____ | 4  |
| 7 )  | 161928      | / | 53976     | = | _____ | 5  |
| 8 )  | 79293305    | / | 7577      | = | _____ | 6  |
| 9 )  | 4084213868  | / | 92        | = | _____ | 7  |
| 10 ) | 565131600   | / | 843480    | = | _____ | 8  |
| 11 ) | 8202972036  | / | 403948    | = | _____ | 9  |
| 12 ) | 91890422386 | / | 350726803 | = | _____ | 11 |

For Q13-22, find the missing number.  
Each answer is an exact integer.

- |      |   |     |       |    |
|------|---|-----|-------|----|
| 13 ) | $17 \times 14 \times ? = 21658$                               | ? = | _____ | 6  |
| 14 ) | $89 \times 24 \times ? = 1593456$                             | ? = | _____ | 8  |
| 15 ) | $47 \times 159 \times ? = 1599222$                            | ? = | _____ | 10 |
| 16 ) | $451 \times 408 \times ? = 66794904$                          | ? = | _____ | 12 |
| 17 ) | $703 \times 473 \times ? = 3184201944$                        | ? = | _____ | 19 |
| 18 ) | $77 \times 60 \times 11 \times ? = 1626240$                   | ? = | _____ | 9  |
| 19 ) | $46 \times 43 \times 245 \times ? = 254420250$                | ? = | _____ | 15 |
| 20 ) | $287 \times 340 \times 562 \times ? = 53688320840$            | ? = | _____ | 18 |
| 21 ) | $70 \times 28 \times 52 \times 25 \times ? = 196196000$       | ? = | _____ | 14 |
| 22 ) | $81 \times 58 \times 971 \times 865 \times ? = 3657868461090$ | ? = | _____ | 28 |

Total value: 200

**SECTION 4: APPROXIMATE MULTIPLICATIONS**

For Q1-6, give the answer to the nearest integer.

- |     |       |   |           |   |       |    |
|-----|-------|---|-----------|---|-------|----|
| 1 ) | 1.1   | x | 1.5       | = | _____ | 3  |
| 2 ) | 5.9   | x | 7.5       | = | _____ | 4  |
| 3 ) | 9.3   | x | 57.6      | = | _____ | 7  |
| 4 ) | 64.5  | x | 82.3      | = | _____ | 8  |
| 5 ) | 27.2  | x | 8965.8    | = | _____ | 12 |
| 6 ) | 509.5 | x | 9776889.1 | = | _____ | 23 |

For Q7-9, give the answer to four significant figures.

- |     |      |   |        |   |       |    |       |    |
|-----|------|---|--------|---|-------|----|-------|----|
| 7 ) | 1.3  | x | 1231.6 | = | _____ | 9  |       |    |
| 8 ) | 98.1 | x | 1626.1 | = | _____ | 12 |       |    |
| 9 ) | 12.9 | x | 83.05  | x | 844.4 | =  | _____ | 38 |

For Q10-12, give the answer to five significant figures.

- |      |       |   |         |   |       |    |       |    |
|------|-------|---|---------|---|-------|----|-------|----|
| 10 ) | 92.96 | x | 887.36  | = | _____ | 14 |       |    |
| 11 ) | 39.11 | x | 30761.7 | = | _____ | 19 |       |    |
| 12 ) | 492.9 | x | 37.71   | x | 248.3 | =  | _____ | 51 |

Total value: 200

## **SECTION 5: APPROXIMATE DIVISIONS**

For Q1-8, give the answer to the nearest integer.

For example,  $13 / 3 = 4$  or  $85 / 8 = 11$

- |     |              |   |            |   |       |    |
|-----|--------------|---|------------|---|-------|----|
| 1 ) | 14           | / | 4          | = | _____ | 2  |
| 2 ) | 410          | / | 6          | = | _____ | 3  |
| 3 ) | 9676         | / | 27         | = | _____ | 4  |
| 4 ) | 2532         | / | 635        | = | _____ | 5  |
| 5 ) | 924440       | / | 47         | = | _____ | 6  |
| 6 ) | 1664085      | / | 86533      | = | _____ | 9  |
| 7 ) | 94533887579  | / | 10908      | = | _____ | 13 |
| 8 ) | 382888859368 | / | 6222627031 | = | _____ | 16 |

For Q9-12, give the answer to four significant figures.

- |      |             |   |        |   |       |    |
|------|-------------|---|--------|---|-------|----|
| 9 )  | 3507.1575   | / | 64.2   | = | _____ | 10 |
| 10 ) | 187520.425  | / | 21.46  | = | _____ | 12 |
| 11 ) | 4752115.53  | / | 7226.1 | = | _____ | 12 |
| 12 ) | 432221.9189 | / | 6218.4 | = | _____ | 13 |

For Q13-15, give the answer to six significant figures.

- |      |               |   |         |   |       |    |
|------|---------------|---|---------|---|-------|----|
| 13 ) | 3615105.0379  | / | 791.7   | = | _____ | 30 |
| 14 ) | 567765.20858  | / | 807.94  | = | _____ | 30 |
| 15 ) | 5450078.94701 | / | 6436.17 | = | _____ | 35 |

Total value: 200



## **SECTION 6: PRIME FACTORS**

Specify each number as the product of prime factors. Factors must be recorded the relevant number of times, although the order does not matter.

For example, 84: 2, 2, 3, 7 and 7, 2, 3, 2 are both correct, but 2, 3, 7 is not.

No prime factor greater than 13 is used in this section

- |     |       |       |   |
|-----|-------|-------|---|
| 1 ) | 66    | _____ | 1 |
| 2 ) | 700   | _____ | 2 |
| 3 ) | 8712  | _____ | 3 |
| 4 ) | 52728 | _____ | 5 |

No prime factor greater than 19 is used in this section

- |     |         |       |    |
|-----|---------|-------|----|
| 5 ) | 8085    | _____ | 6  |
| 6 ) | 72618   | _____ | 8  |
| 7 ) | 750750  | _____ | 11 |
| 8 ) | 5140443 | _____ | 15 |

No prime factor greater than 41 is used in this section

- |      |          |       |    |
|------|----------|-------|----|
| 9 )  | 74865    | _____ | 11 |
| 10 ) | 309225   | _____ | 16 |
| 11 ) | 4370938  | _____ | 22 |
| 12 ) | 85840209 | _____ | 30 |

For Q13-14, each is the product of 4 (not necessarily different) 2-digit primes.

- |      |         |       |    |
|------|---------|-------|----|
| 13 ) | 1827971 | _____ | 35 |
| 14 ) | 3039107 | _____ | 35 |

Total value: 200

**SECTION 7A: FRACTION ADDITIONS**

1 ) 4 2 ### 3 + 3 1 / 3 0 1 = \_\_\_\_\_ 2

2 ) 7 2 ### 7 + 11 5 / 6 0 1 = \_\_\_\_\_ 3

3 ) 24 1 ### 2 + 12 4 / 5 0 1 = \_\_\_\_\_ 4

4 ) 13 3 ### 13 + 36 21 / 22 0 1 = \_\_\_\_\_ 6

5 ) 16 4 ### 21 + 21 25 / 32 + 23 4 / 9 = \_\_\_\_\_ 10

6 ) 29 25 ### 34 + 25 50 / 81 + 33 6 / 19 = \_\_\_\_\_ 24

7 ) 89 57 ### 116 + 56 39 / 119 + 73 13 / 48 = \_\_\_\_\_ 38

Total value: 87

**SECTION 7B: FRACTION SUBTRACTIONS**

1 )  $2 \frac{5}{9} - 1 \frac{2}{5} = \underline{\hspace{2cm}}$  2

2 )  $19 \frac{19}{37} - 18 \frac{24}{43} = \underline{\hspace{2cm}}$  4

3 )  $36 \frac{1}{3} - 22 \frac{11}{34} = \underline{\hspace{2cm}}$  5

4 )  $90 \frac{36}{65} - 59 \frac{49}{89} = \underline{\hspace{2cm}}$  6

5 )  $418 \frac{83}{192} - 397 \frac{13}{30} = \underline{\hspace{2cm}}$  11

Total value: 28

**SECTION 7C: FRACTION ADDITIONS & SUBTRACTIONS MIXED**

1 ) 5 3 / 4 - 3 7 / 8 + 5 5 / 7 = \_\_\_\_\_ 4

2 ) 18 7 / 8 - 17 14 / 15 + 9 5 / 7 = \_\_\_\_\_ 7

3 ) 15 1 / 2 - 10 1 / 4 + 18 3 / 4 = \_\_\_\_\_ 11

4 ) 35 26 / 37 - 29 2 / 3 + 22 2 / 9 = \_\_\_\_\_ 18

5 ) 29 7 / 8 - 22 1 / 2 + 19 7 / 11 = \_\_\_\_\_ 18

6 ) 27 29 / 30 - 27 45 / 89 + 29 19 / 45 = \_\_\_\_\_ 27

Total value: 85

**SECTION 8A: FRACTION MULTIPLICATIONS**

1)    3        1 / 5        x    1        1 / 2        =    \_\_\_\_\_    2

2)    12        1 / 3        x    8        2 / 11        =    \_\_\_\_\_    5

3)    85        13 / 53        x    70        1 / 7        =    \_\_\_\_\_    25

4)    137        31 / 41        x    137        10 / 33        =    \_\_\_\_\_    48

5)    2        5 / 6        x    3        5 / 6        x    2        3 / 10        =    \_\_\_\_\_    7

6)    12        5 / 11        x    5        6 / 13        x    5        1 / 3        =    \_\_\_\_\_    17

7)    11        5 / 6        x    22        3 / 8        x    7        5 / 19        =    \_\_\_\_\_    40

Total value: 144

**SECTION 8B: FRACTION DIVISIONS**

1 )      7      7 / 9      /      2      1 / 2      =      \_\_\_\_\_      3

2 )      48      21 / 23      /      6      15 / 23      =      \_\_\_\_\_      9

3 )      135      67 / 135      /      10      19 / 25      =      \_\_\_\_\_      13

4 )      464      161 / 335      /      20      37 / 67      =      \_\_\_\_\_      31

Total value:      56

**SECTION 9A: CALENDAR CALCULATIONS**

For Q1-3, enter the correct weekday (eg. *Saturday* or *Sat*).

- 1 ) June 8, 1904 \_\_\_\_\_ 2
- 2 ) October 10, 1935 \_\_\_\_\_ 2
- 3 ) July 15, 2037 \_\_\_\_\_ 2

For Q4-6, enter the correct date in the specified month.

- 4 ) Fifth Wednesday in August 2012 = Day No. \_\_\_\_\_ 3
- 5 ) Fourth Saturday in July 1945 = Day No. \_\_\_\_\_ 3
- 6 ) First Friday in July 2080 = Day No. \_\_\_\_\_ 3

For Q7-9, insert any month for which the equation is correct (eg. *October* or *Oct*). The solution is not necessarily unique; however only one answer is required in each case.

- 7 ) Day 26 of the month in 2082 = Monday \_\_\_\_\_ 6
- 8 ) Day 16 of the month in 1920 = Thursday \_\_\_\_\_ 6
- 9 ) Day 4 of the month in 2064 = Tuesday \_\_\_\_\_ 6

For Q10-12, insert the largest year less than or equal to 1968 (inclusive) for which the equation is correct. For example, if the equation works with years 1963 and 1967, then only 1967 is the correct answer.

- 10 ) October 14 = Thursday \_\_\_\_\_ 12
- 11 ) September 25 = Monday \_\_\_\_\_ 12
- 12 ) March 6 = Friday \_\_\_\_\_ 12

Total value: 69

**SECTION 9B: TIME CALCULATIONS**

For Q1-5, give the time in seconds between the given dates and times.  
The start & finish dates are the same unless otherwise stated.

- 1 ) From 8:29:13 on May 11, 1976 to 23:06:59 on May 11, 1976 \_\_\_\_\_ 6
- 2 ) From 0:58:41 on February 7, 1954 to 14:11:56 on February 12, 1954 \_\_\_\_\_ 10
- 3 ) From 10:07:21 on June 11, 1988 to 15:26:05 on July 26, 1988 \_\_\_\_\_ 16
- 4 ) From 15:54:16 on April 16, 1975 to 11:46:34 on March 14, 1976 \_\_\_\_\_ 28
- 5 ) From 16:08:59 on April 16, 2032 to 16:20:22 on September 5, 2037 \_\_\_\_\_ 36

For Q6-10, convert the given period of time into the required scale, correct to 4 significant figures.

- 6 ) 155100 minutes in hours \_\_\_\_\_ 7
  - 7 ) 22930 minutes in seconds \_\_\_\_\_ 7
  - 8 ) 819.2 hours in seconds \_\_\_\_\_ 7
  - 9 ) 88.28 days in minutes \_\_\_\_\_ 7
  - 10 ) 23450 minutes in hours \_\_\_\_\_ 7
- Total value: 131



**SECTION 10: MISCELLANEOUS (ALGEBRAIC, NEXT SQUARES/CUBES, REMAINDERS)**

For Q1-3, give x to 4 significant figures.

- |     |                      |     |       |    |
|-----|----------------------|-----|-------|----|
| 1 ) | $1/6 - 1/21 = 1/x$   | x = | _____ | 4  |
| 2 ) | $1/23 - 1/37 = 1/x$  | x = | _____ | 8  |
| 3 ) | $1/69 - 1/117 = 1/x$ | x = | _____ | 15 |

For Q4-8, give the next exact square after the given number.

For example, the next exact square after 222 is 225 (which is  $15_2$ ); only the number is required, ie "225".

- |     |                                     |             |       |    |
|-----|-------------------------------------|-------------|-------|----|
| 4 ) | What is the next exact square after | 800 ?       | _____ | 1  |
| 5 ) | What is the next exact square after | 99187 ?     | _____ | 7  |
| 6 ) | What is the next exact square after | 596399 ?    | _____ | 11 |
| 7 ) | What is the next exact square after | 1767787 ?   | _____ | 17 |
| 8 ) | What is the next exact square after | 784505499 ? | _____ | 25 |

For Q9-12, give the next exact cube after the given number.

For example, the next exact cube after 222 is 343 (which is  $7_3$ ); only the number is required, ie "343".

- |      |                                   |             |       |    |
|------|-----------------------------------|-------------|-------|----|
| 9 )  | What is the next exact cube after | 355 ?       | _____ | 1  |
| 10 ) | What is the next exact cube after | 170994 ?    | _____ | 12 |
| 11 ) | What is the next exact cube after | 6754763 ?   | _____ | 18 |
| 12 ) | What is the next exact cube after | 890969936 ? | _____ | 37 |

For Q13-18, give the remainder after dividing the two integer values.

For example, the remainder of  $553 / 6$  is 1 (because  $553 = \{92 \times 6\} + 1$ ).

- |      |          |   |     |             |       |    |
|------|----------|---|-----|-------------|-------|----|
| 13 ) | 86       | / | 9   | Remainder = | _____ | 1  |
| 14 ) | 591      | / | 16  | Remainder = | _____ | 2  |
| 15 ) | 5174     | / | 64  | Remainder = | _____ | 4  |
| 16 ) | 67155    | / | 46  | Remainder = | _____ | 8  |
| 17 ) | 680758   | / | 592 | Remainder = | _____ | 12 |
| 18 ) | 33829811 | / | 53  | Remainder = | _____ | 17 |

Total value: 200

## **SECTION 11A: EXACT ROOTS**

All the answers in this section are integers.

|      |                |                    |   |       |    |
|------|----------------|--------------------|---|-------|----|
| 1 )  | Square root of | 676                | = | _____ | 1  |
| 2 )  | Square root of | 3600               | = | _____ | 1  |
| 3 )  | Square root of | 45369              | = | _____ | 2  |
| 4 )  | Square root of | 9265936            | = | _____ | 3  |
| 5 )  | Square root of | 54730404           | = | _____ | 3  |
| 6 )  | Square root of | 7491075601         | = | _____ | 5  |
| 7 )  | Cube root of   | 5832               | = | _____ | 1  |
| 8 )  | Cube root of   | 778688             | = | _____ | 2  |
| 9 )  | Cube root of   | 1520875            | = | _____ | 3  |
| 10 ) | Cube root of   | 521660125          | = | _____ | 4  |
| 11 ) | Cube root of   | 34075248488        | = | _____ | 6  |
| 12 ) | 5 th root of   | 59049              | = | _____ | 2  |
| 13 ) | 7 th root of   | 4902227890625      | = | _____ | 10 |
| 14 ) | 5 th root of   | 1889568            | = | _____ | 3  |
| 15 ) | 7 th root of   | 2097152            | = | _____ | 5  |
| 16 ) | 4 th root of   | 58573800926022001  | = | _____ | 8  |
| 17 ) | 6 th root of   | 172358602780396096 | = | _____ | 9  |
| 18 ) | 7 th root of   | 536143015838069981 | = | _____ | 7  |

Total value: 75

**SECTION 11B: INEXACT ROOTS**

For Q1-10, give the answer to the nearest integer.

For example, square root of 28 = 5 or cube root of 47 = 4.

|      |                |          |   |       |   |
|------|----------------|----------|---|-------|---|
| 1 )  | Square root of | 26       | = | _____ | 1 |
| 2 )  | Square root of | 113      | = | _____ | 1 |
| 3 )  | Square root of | 21726    | = | _____ | 3 |
| 4 )  | Cube root of   | 364      | = | _____ | 1 |
| 5 )  | Cube root of   | 7212     | = | _____ | 2 |
| 6 )  | Cube root of   | 511      | = | _____ | 2 |
| 7 )  | 5 th root of   | 46569    | = | _____ | 4 |
| 8 )  | 4 th root of   | 37007967 | = | _____ | 6 |
| 9 )  | 7 th root of   | 724157   | = | _____ | 8 |
| 10 ) | 7 th root of   | 13896291 | = | _____ | 5 |

For Q11-16, give the answer to 3 significant figures.

|      |                |        |   |       |   |
|------|----------------|--------|---|-------|---|
| 11 ) | Square root of | 638    | = | _____ | 3 |
| 12 ) | Cube root of   | 5115   | = | _____ | 6 |
| 13 ) | 4 th root of   | 933492 | = | _____ | 9 |
| 14 ) | 6 th root of   | 1609   | = | _____ | 9 |
| 15 ) | 5 th root of   | 68792  | = | _____ | 9 |
| 16 ) | 4 th root of   | 149880 | = | _____ | 9 |

For Q17-20, give the answer to 2 decimal places.

|      |              |        |   |       |    |
|------|--------------|--------|---|-------|----|
| 17 ) | 4 th root of | 4857   | = | _____ | 8  |
| 18 ) | 6 th root of | 5296   | = | _____ | 10 |
| 19 ) | 7 th root of | 5963   | = | _____ | 13 |
| 20 ) | 6 th root of | 528753 | = | _____ | 16 |

Total value: 125

**SECTION 12: BASE CONVERSIONS**

In each of the first 15 problems, your task is to convert a number from one base to another. No base higher than 16 will be used in any of these problems. For bases higher than 10, the character 'A' represents a unit count of 10, 'B' a count of 11, 'C' represents 12, 'D' represents 13, 'E' shows 14, and 'F' shows a value of 15.

- 1 ) Convert      440                      from base      5            into base      6                      \_\_\_\_\_                      2
- 2 ) Convert      A2A                      from base      11           into base      5                      \_\_\_\_\_                      6
- 3 ) Convert      8458                      from base      10           into base      15                      \_\_\_\_\_                      17
- 4 ) Convert      6385                      from base      11           into base      14                      \_\_\_\_\_                      8
- 5 ) Convert      21323554                      from base      7            into base      13                      \_\_\_\_\_                      12
- 6 ) Convert      2DC4                      from base      14           into base      10                      \_\_\_\_\_                      17

Add the following numbers in their given bases, giving the answer in base 10 in each case.

- 7 ) A                      (base 15) + 33                      (base 16) =                      (in base 10)                      \_\_\_\_\_                      5
- 8 ) 782                      (base 11) + 43                      (base 14) =                      (in base 10)                      \_\_\_\_\_                      13
- 9 ) 83                      (base 11) + 4CA                      (base 14) =                      (in base 10)                      \_\_\_\_\_                      14
- 10 ) B223                      (base 12) + AC6                      (base 16) =                      (in base 10)                      \_\_\_\_\_                      21

Multiply the following numbers in their given bases, giving the answer in base 10 in each case.

- 11 ) 342                      (base 9) x 4203113                      (base 5) =                      (in base 10)                      \_\_\_\_\_                      22
- 12 ) 75                      (base 13) x 76                      (base 15) =                      (in base 10)                      \_\_\_\_\_                      30
- 13 ) 6A8                      (base 12) x 506065                      (base 7) =                      (in base 10)                      \_\_\_\_\_                      33

Total value:                      200

**SECTION 13: SUMS OF SQUARES**

Each of the following is the sum of 2, 3 or 4 exact squares.  
There may be more than one answer; only one is required in each case.  
Zeros may not be used, and at least two numbers must be given.  
Please give the numbers to be squared, not the actual squares.

Example:  $144 = 6^2 + 6^2 + 6^2 + 6^2$ , and so the answer '6, 6, 6, 6' is correct.  
The answers '36+36+36+36', '12^2' and '12^2+0^2' will not be accepted.

|      |         |       |    |
|------|---------|-------|----|
| 1 )  | 900     | _____ | 2  |
| 2 )  | 664     | _____ | 2  |
| 3 )  | 745     | _____ | 2  |
| 4 )  | 767     | _____ | 2  |
| 5 )  | 753     | _____ | 2  |
| 6 )  | 759     | _____ | 2  |
| 7 )  | 3885    | _____ | 4  |
| 8 )  | 4974    | _____ | 4  |
| 9 )  | 8983    | _____ | 4  |
| 10 ) | 3748    | _____ | 4  |
| 11 ) | 9546    | _____ | 4  |
| 12 ) | 62550   | _____ | 7  |
| 13 ) | 58559   | _____ | 7  |
| 14 ) | 60137   | _____ | 7  |
| 15 ) | 92773   | _____ | 7  |
| 16 ) | 170970  | _____ | 14 |
| 17 ) | 146031  | _____ | 14 |
| 18 ) | 712902  | _____ | 14 |
| 19 ) | 779706  | _____ | 14 |
| 20 ) | 8411101 | _____ | 28 |
| 21 ) | 5452611 | _____ | 28 |
| 22 ) | 4435757 | _____ | 28 |

Total value: 200

**SECTION 14: BRACKETS**

- 1 )  $(51 + 44) \times (49 + 46)$  = \_\_\_\_\_ 3
- 2 )  $(53 + 56) \times (61 + 45)$  = \_\_\_\_\_ 3
- 3 )  $((578 - 8) / 38) \times (137 + 738)$  = \_\_\_\_\_ 4
- 4 )  $((727 - 7) / 16) \times (328 + 168)$  = \_\_\_\_\_ 4
- 5 )  $((858 - 3) / 57) \times (655 + 232)$  = \_\_\_\_\_ 4
- 6 )  $((877 - 77) / 16) \times (7465 + 711)$  = \_\_\_\_\_ 5
- 7 )  $((896 - 64) / 16) \times (6276 + 437)$  = \_\_\_\_\_ 5
- 8 )  $(69 + (4 \times 89)) \times (650 - 98)$  = \_\_\_\_\_ 7
- 9 )  $(74 + (9 \times 57)) \times (912 - 95)$  = \_\_\_\_\_ 7
- 10 )  $(99 + (2 \times 97)) \times (641 - 76)$  = \_\_\_\_\_ 7
- 11 )  $((5192 - 44) / 26) \times (2885 + 1129)$  = \_\_\_\_\_ 11
- 12 )  $((4822 - 70) / 24) \times (2317 + 3658)$  = \_\_\_\_\_ 11
- 13 )  $(84 + (42 \times 87)) \times (9441 - 81)$  = \_\_\_\_\_ 16
- 14 )  $(52 + (50 \times 56)) \times (9921 - 64)$  = \_\_\_\_\_ 16
- 
- 15 )  $((3 \frac{1}{8} + 4 \frac{2}{7}) \times 7 \frac{1}{2})$  = \_\_\_\_\_ 8
- 16 )  $(3 \frac{1}{4} + 6 \frac{3}{5}) \times (4 \frac{1}{3} + 7 \frac{3}{8})$  = \_\_\_\_\_ 12
- 17 )  $(4 \frac{1}{3} + 7 \frac{2}{5}) \times (5 \frac{1}{6} + 7 \frac{2}{7})$  = \_\_\_\_\_ 15
- 18 )  $(7 \frac{1}{3} + 3 \frac{1}{6} + 7 \frac{1}{6}) \times (3 \frac{3}{5} + 3 \frac{3}{8})$  = \_\_\_\_\_ 25
- 19 )  $(6 \frac{1}{5} + 4 \frac{3}{5} + 6 \frac{1}{7}) \times (3 \frac{3}{10} + 5 \frac{1}{3} + 4 \frac{1}{4})$  = \_\_\_\_\_ 37

Total value: 200

**SECTION 15: VALUE COMPARISONS**

Place the following numbers in order of increasing value

- 1 ) 12/17, 0.555, 46/73, 16/21, 12/25 = \_\_\_\_\_ 6
- 2 ) 24/37, 45/64, 15/32, 0.590, 41/78 = \_\_\_\_\_ 6
- 3 ) 14/27, 17/29, 46/59, 0.685, 17/38, 0.831 = \_\_\_\_\_ 8
- 4 ) 0.366, 9/16, 20/43, 0.631, 53/68, 5/7 = \_\_\_\_\_ 8
- 5 ) 31/45, 31/40, 21/34, 76/87, 13/25 = \_\_\_\_\_ 9
- 6 ) 32/57, 17/28, 5/11, 26/35, 7/10 = \_\_\_\_\_ 9
- 7 ) 38/83, 10/13, 0.504, 47/70, 10/17, 64/77 = \_\_\_\_\_ 10
- 8 ) 46/89, 68/95, 41/70, 11/26, 11/17, 0.773 = \_\_\_\_\_ 10
- 9 ) 47/83, 8/19, 27/41, 18/25, 23/29, 12/25 = \_\_\_\_\_ 12
- 10 ) 20/29, 8/21, 57/97, 71/92, 37/76, 9/14 = \_\_\_\_\_ 12
- 11 ) 26/33, 15/44, 19/30, 4/7, 26/37, 13/32, 46/97 = \_\_\_\_\_ 15
- 12 ) 29/49, 12/23, 27/58, 2/3, 14/37, 31/41, 5/18 = \_\_\_\_\_ 15
- 13 ) 19/29, 55/68, 11/15, 6/17, 37/65, 43/90, 15/49, 3/7 = \_\_\_\_\_ 18
- 14 ) 9/13, 4/9, 3/5, 10/13, 47/93, 11/28, 20/31, 2/7 = \_\_\_\_\_ 18
- 15 ) 19/31, 31/56, 64/91, 20/63, 7/29, 58/73, 7/15, 19/48, 49/57 = \_\_\_\_\_ 22
- 16 ) 15/43, 6/25, 16/27, 31/69, 11/39, 22/31, 28/43, 13/24, 24/31 = \_\_\_\_\_ 22

Total value: 200

**SECTION 16: MISCELLANEOUS QUESTIONS, PART 2**

Q 1-4: Simultaneous equations.

Each answer consists of exact integer values which may be listed in any order.

- |     |   |             |       |    |
|-----|---|-------------|-------|----|
| 1 ) | $A + B = 13, A^2 + B^2 = 85$            | A =, B=     | _____ | 2  |
| 2 ) | $A + B = 46, A^2 + B^2 = 1130$          | A =, B=     | _____ | 4  |
| 3 ) | $A + B = 60, A^2 + B^2 = 2138$          | A =, B=     | _____ | 8  |
| 4 ) | $A + B + C = 40, A^2 + B^2 + C^2 = 664$ | A =, B=, C= | _____ | 28 |

Q 5-8: Powers of fractions.

Give the result of each equation to the nearest integer.

- |     |                   |   |       |    |
|-----|-------------------|---|-------|----|
| 5 ) | $1 \frac{1}{3}^3$ | = | _____ | 1  |
| 6 ) | $2 \frac{3}{4}^3$ | = | _____ | 4  |
| 7 ) | $3 \frac{5}{6}^4$ | = | _____ | 10 |
| 8 ) | $4 \frac{8}{9}^4$ | = | _____ | 17 |

Q 9-12: Geometry.

Volume of a cone:  $\frac{1}{3} \pi r^2 h$                       Take the value of pi as 3.1416  
 Volume of a sphere:  $\frac{4}{3} \pi r^3$   
 Right-angled triangle:  $A^2 + B^2 = C^2$   
 Volume of a pyramid:  $\frac{1}{3} \text{base (lw) h}$

Give the answer to each of the following (Q9-11) to the nearest integer.

- |      |   |              |       |    |
|------|---|--------------|-------|----|
| 9 )  | Hypotenuse of a triangle: A = 412, B = 60 | Hypotenuse = | _____ | 9  |
| 10 ) | Volume of a sphere: r = 29                | Volume =     | _____ | 12 |
| 11 ) | Volume of a cone: r = 12, h = 19          | Volume =     | _____ | 14 |

Give the answer to Q12 as an exact fraction, or as an integer if appropriate.

- |      |  |          |       |    |
|------|--|----------|-------|----|
| 12 ) | Volume of a pyramid: l = 134 w = 375 h = 451 | Volume = | _____ | 13 |
|------|--|----------|-------|----|

Q 13-18: Ratio calculations.

Each of the following has an exact answer.

- |      |                                     |     |       |    |
|------|-------------------------------------|-----|-------|----|
| 13 ) | $43 / X = 215 / 2150$               | X = | _____ | 2  |
| 14 ) | $215 / 7955 = 3010 / X$             | X = | _____ | 3  |
| 15 ) | $1585 / 155705 = 15850 / X$         | X = | _____ | 5  |
| 16 ) | $6748 / 1275372 = 121464 / X$       | X = | _____ | 8  |
| 17 ) | $X / 13306680 = 809190 / 239520240$ | X = | _____ | 11 |
| 18 ) | $X / 2449185 = 467904 / 156747840$  | X = | _____ | 13 |

Q 19-24: Missing information.

Fill in the missing information in each case.  
 The symbol '?' shows one missing digit.  
 The symbol '#' shows any number of missing digits.

- |      |   |       |    |
|------|---|-------|----|
| 19 ) | $7224 / \# = 84$                                  | _____ | 2  |
| 20 ) | $53^2 + 18^2 = 3??3$                              | _____ | 3  |
| 21 ) | Cube root of 421875000 = ??0                      | _____ | 3  |
| 22 ) | $91376 + 3774 - \# = 48705$                       | _____ | 4  |
| 23 ) | $(30 + (9 \times \#)) \times (897 - 63) = 227682$ | _____ | 12 |
| 24 ) | $1470 \times 900 / 6300 = \#$                     | _____ | 12 |



**SECTION 17: EXTENSIONS TO PREVIOUS SECTIONS**

For Q1 – Q7, all answers are required to their full accuracy.

- 1 )  $7460254117957 + 3307078197031 + 4643575910023 + 8897949032205 + 5533388107340 + 3260027917054$  = \_\_\_\_\_ 15
- 2 )  $238259813536218 - 158168241867183$  = \_\_\_\_\_ 6
- 3 )  $3174712.76876 + 6215464.1449 + 7702115.8119 + 79819075.6521 + 9303042.4343 + 2485093.65106$  = \_\_\_\_\_ 12
- 4 )  $3145625617 - 1027028528 + 1653275479 - 1204420714 + 6709092643 - 4103266647$  = \_\_\_\_\_ 17
- 5 )  $1990 \times 34071 \times 92485$  = \_\_\_\_\_ 50
- 6 )  $509571337834282 / 214646730343$  = \_\_\_\_\_ 18
- 7 )  $82 \times 435 \times 718 \times 382 \times ? = 1868634159720$  ? = \_\_\_\_\_ 32

For Q8, give your answer to the nearest integer.

- 8 )  $42814683.8 \times 9524105.2$  = \_\_\_\_\_ 50

For Q9, give your answer to 6 significant figures

- 9 )  $194413601.75 / 7.387349$  = \_\_\_\_\_ 50

For Q10, give the prime factors of the number. No prime factor greater than 107 is used.

- 10 ) 920351061 \_\_\_\_\_ 50

For Q11-13, give each answer in its simplest form.

- 11 )  $411 \frac{71}{156} - 405 \frac{41}{94}$  = \_\_\_\_\_ 20
- 12 )  $89 \frac{74}{121} - 42 \frac{65}{142} + 88 \frac{47}{52}$  = \_\_\_\_\_ 30
- 13 )  $199 \frac{17}{21} \times 198 \frac{25}{42}$  = \_\_\_\_\_ 50 1

Amount of time passed: For Q14, give the exact number of seconds between the two moments stated.

- 14 ) From 15:02:06 on August 6, 1919 to 13:33:05 on November 19, 1927 \_\_\_\_\_ 50

For Q15, give x to 4 significant figures.

- 15 )  $1/69 - 1/144 = 1/x$  x = \_\_\_\_\_ 20
- 16 ) What is the remainder following the inexact integer division of  $118516005 / 514$  \_\_\_\_\_ 30
- 17 ) What is the exact cube root of 685942283173888? \_\_\_\_\_ 19
- 18 ) What is the 7th root of 9621 to three significant figures? \_\_\_\_\_ 13
- 19 ) What is the 9th root of 792601750 to two decimal places? \_\_\_\_\_ 18
- 20 )  $6840A$  (base 12)  $\times$   $9A30$  (base 14) = (in base 10) \_\_\_\_\_ 50

Q21 is the sum of 2, 3 or 4 exact squares. There may be more than one answer; only one is required. Zeros may not be used, and at least two numbers must be given. Give the numbers to be squared, not the actual squares.

- 21 ) 33153214 \_\_\_\_\_ 50
- 22 )  $(79 + (95 \times 79)) \times (36662 - 10409)$  = \_\_\_\_\_ 25
- 23 )  $(99 + (94 \times 94)) \times (49003 - 15517)$  = \_\_\_\_\_ 25

For Q24-26, place the numbers in order of increasing value.

- 24 )  $47/59, 0.710, 11/25, 1/2, 53/86, 31/54$  \_\_\_\_\_ 10
- 25 )  $5/18, 20/47, 5/8, 67/89, 41/83, 19/52, 13/19, 51/91$  \_\_\_\_\_ 18
- 26 )  $29/45, 40/97, 44/87, 47/86, 33/46, 31/38, 7/39, 4/11, 13/47$  \_\_\_\_\_ 22

For Q27, calculate the value to the nearest integer

- 27 )  $5 \frac{9}{10} ^ 5$  = \_\_\_\_\_ 35
- 28 )  $3528 \times 1904 / 17136$  = \_\_\_\_\_ 15

Total value: 800

**SECTION 18: SURPRISE TASKS**

1 ) Give the mod 101 of  $2^{50}$  \_\_\_\_\_ 20

2 ) How many figures does  $97^{97}$  have? \_\_\_\_\_ 20

Total value: 40

**SUMMARY OF THE TEST PAPER:**

| Section | Subject                          | Questions | Total value |
|---------|----------------------------------|-----------|-------------|
| 1A      | Integer Additions                | 13        | 47          |
| 1B      | Integer Subtractions             | 18        | 47          |
| 1C      | Decimal Additions & Subtractions | 18        | 47          |
| 1D      | Mixed Additions & Subtractions   | 15        | 59          |
| 2       | Integer Multiplications          | 20        | 200         |
| 3       | Exact Divisions                  | 22        | 200         |
| 4       | Approximate Multiplications      | 12        | 200         |
| 5       | Approximate Divisions            | 15        | 200         |
| 6       | Prime Factors                    | 14        | 200         |
| 7A      | Fraction Additions               | 7         | 87          |
| 7B      | Fraction Subtractions            | 5         | 28          |
| 7C      | Fraction Adds & Subs Mixed       | 6         | 85          |
| 8A      | Fraction Multiplications         | 7         | 144         |
| 8B      | Fraction Divisions               | 4         | 56          |
| 9A      | Calendar Calculations            | 12        | 69          |
| 9B      | Time Calculations                | 10        | 131         |
| 10      | Miscellaneous                    | 18        | 200         |
| 11A     | Exact Roots                      | 18        | 75          |
| 11B     | Inexact Roots                    | 20        | 125         |
| 12      | Base Conversions                 | 13        | 200         |
| 13      | Sums of Squares                  | 22        | 200         |
| 14      | Brackets                         | 19        | 200         |
| 15      | Value Comparisons                | 16        | 200         |
| 16      | Miscellaneous 2                  | 24        | 200         |
| 17      | Extensions                       | 28        | 800         |
| 18      | Surprise Tasks                   | 2         | 40          |
| TOTAL   |                                  | 378       | 4040        |